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| Obuda University John von Neumann Faculty of Informatics | | Institute of Applied Mathematics | | |
| Name and code: <i>Analysis</i> NMXAN1PMNE | | Credits: <i>2021/22 year I. semester</i> | | |
| Subject lecturers: Dr. Zoltán Léka | | | | |
| Prerequisites (with code): | | - | | |
| Weekly hours: | Lecture: 2 | Seminar.: 1 | Lab. hours: 0 | Consultation: 0 |
| Way of assessment: | Final grade based on two midterm exams | | | |
| Course description: | | | | |
| <i>Goal:</i> Our goal is to introduce the fundamental concepts of functional analysis and Lebesgue integration. These concepts are crucial in the modern study of probability theory, (partial) differential equations, and quantum theory, for instance. | | | | |
| <i>Course description:</i> The problem of the measure. Lebesgue integral, convergence theorems. Lebesgue and Riemann integrals. Study of Hilbert spaces with orthogonal systems, duality. | | | | |

| Lecture schedule | | | | | |
|-----------------------|---|-----------------------|--------------|---|--|
| <i>Education week</i> | <i>Topic</i> | | | | |
| 1. | Introduction to measure theory | | | | |
| 2. | Exterior measure and Lebesgue measure of \mathbb{R}^d | | | | |
| 3. | Measurable functions and their properties | | | | |
| 4. | Lebesgue integral | | | | |
| 5. | Convergence theorems: Fatou lemma, Monotone convergence theorem and Lebesgue's dominated theorem | | | | |
| 6. | 1 st midterm exam | | | | |
| 7. | General measures and the Lebesgue L_p -spaces | | | | |
| 8. | Differentiation: absolute continuous functions | | | | |
| 9. | Functions of bounded variations | | | | |
| 10. | Introduction to Hilbert spaces, normed spaces | | | | |
| 11. | Geometry of Hilbert spaces, inner product spaces | | | | |
| 12. | Duality, orthogonal basis of L_2 spaces, integral operators, kernels | | | | |
| 13. | 2 nd midterm exam | | | | |
| 14. | Resit exam | | | | |
| Midterm requirements | | | | | |
| | <table><tr><th><i>Education week</i></th><th><i>Topic</i></th></tr><tr><td>-</td><td></td></tr></table> | <i>Education week</i> | <i>Topic</i> | - | |
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Final grade calculation methods

| Achieved result | Grade |
|-----------------|------------------|
| 89%-100% | excellent (5) |
| 76%-88<% | good (4) |
| 63%-75<% | average (3) |
| 51%-62<% | satisfactory (2) |
| 0%-50<% | failed (1) |

Type of exam

To get the signature, one needs to accomplish at least 50% of the weekly home assignments. There will be two written midterms.

Type of replacement

At the last week of the semester one can have a resit exam.

References

Mandatory:

E. Stein: Real Analysis

Recommended:

Rynne and Youngson: Linear Functional Analysis