

Obuda University John von Neumann Faculty of Informatics			Institute of Applied Mathematics		
Name and code: Functional inequalities			Credits: 2021/22 year II. semester		
Subject lecturers: Prof. dr. habil. Alexandru Kristály					
Prerequisites (with code):		Calculus I, II			
Weekly hours:	Lecture:	Seminar.:	Lab. hours:	Consultation:	
Way of assessment:					
Course description:					
Goal: to provide an introduction into functional inequalities arising in Geometric Analysis, Sobolev spaces and PDEs.					
Course description: isoperimetric inequalities; symmetrisation; optimal mass transport; sharp Sobolev inequalities; influence of curvature.					

Lecture schedule	
Education week	Topic
1.	$L^1$ -Sobolev inequalities
2.	Optimal mass transportation: basic elements
3.	Monge-Kantorovich problem
4.	Symmetrisation
5.	Inequality of Polya-Szego
6.	Inequality of Hardy-Littlewood-Polya
7.	Sharp Sobolev inequality I: Talenti approach
8.	Hardy inequality
9.	Heisenberg-Pauli-Weyl uncertainty principle
10.	Brezis-Poincare-Vazquez inequality
11.	Sharp Sobolev inequality II: Cordero-Erausquin-Nazaret-Villani approach
12.	Influence of curvature I: negative curvature
13.	Influence of curvature II: positive curvature
14.	Application to elliptic problems (Dirichlet, Schrodinger)
Midterm requirements	
Education week	Topic
Final grade calculation methods	
Achieved result	Grade
89%-100%	excellent (5)
76%-88<%	good (4)
63%-75<%	average (3)
51%-62<%	satisfactory (2)
0%-50<%	failed (1)

[SK1] megjegyzést írt:

<b>Type of exam</b>
Project presentation & Written exam
<b>Type of replacement</b>
Project presentation
<b>References</b>
Mandatory: <ol style="list-style-type: none"> <li>1. Ghoussoub N., Moradifam A., Functional Inequalities: New Perspectives and New Applications, AMS, 2013.</li> <li>2. Kristály A., Sharp uncertainty principles on Riemannian manifolds: the influence of curvature. J. Math. Pures Appl. (9) 119 (2018), 326–346.</li> </ol>
Recommended: <ol style="list-style-type: none"> <li>1. Kristály A., Radulescu V., Varga Cs., Variational Principles in Mathematical Physics, Geometry, and Economics, Cambridge University Press, Enciclopedia of Mathematics and its Applications. No 136, 2010.</li> <li>2. Balogh Z., Kristály A., Sipos K., Geometric inequalities on Heisenberg groups. Calc. Var. Partial Differential Equations 57 (2018), no. 2, Art. 61, 41 pp.</li> </ol>